

Vortex Coupling in Propulsive Pulsed Jets

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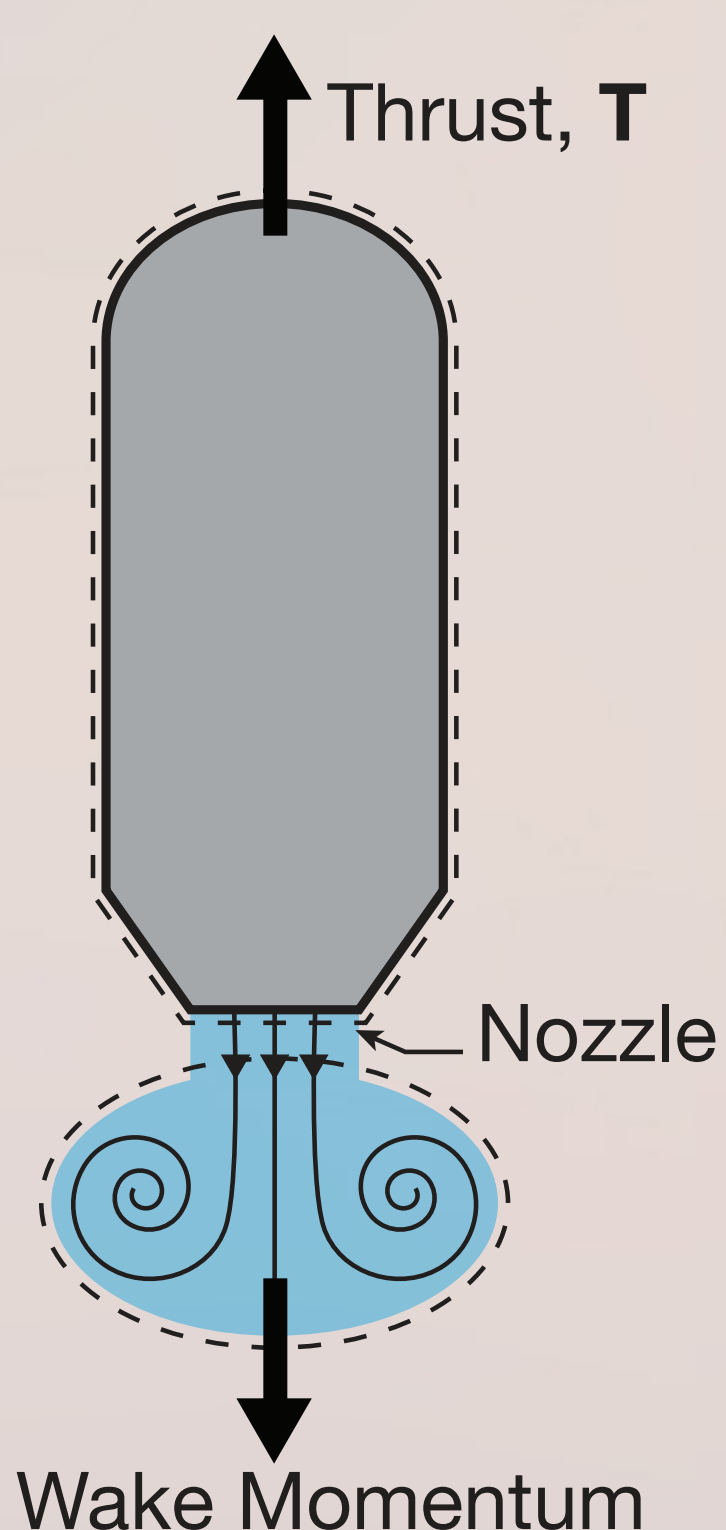
Motivation

For underwater vehicles that need to perform **precise** maneuvers, **pulsed jets** deliver impulse with fine control that can't be matched by propellers.¹

However, for arbitrary motion, vehicles require multiple thrusters that could interact with each other depending on the design.

When jets act simultaneously, how will **hydrodynamic coupling** between nearby jets **affect thrust production**?

Background



- ① Unlike continuous jets, a pulsed jet **initially forms a vortex ring** at the nozzle tip.¹⁻³
- ② Vortex formation introduces a **nozzle overpressure** while the jet is developing.³
- ③ Overpressure relates the thrust to the vortex ring dynamics according to:

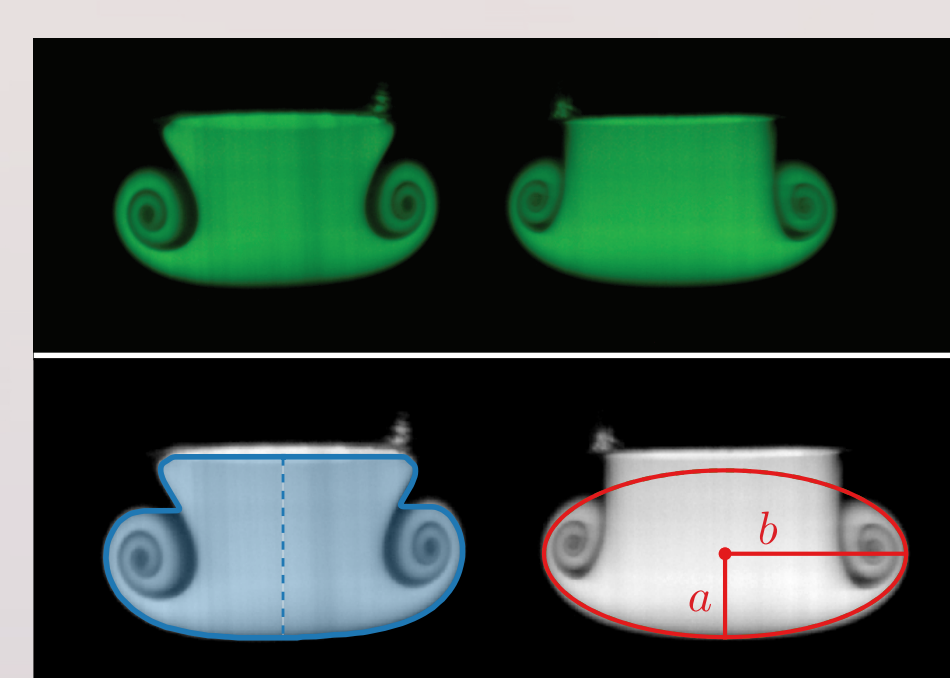
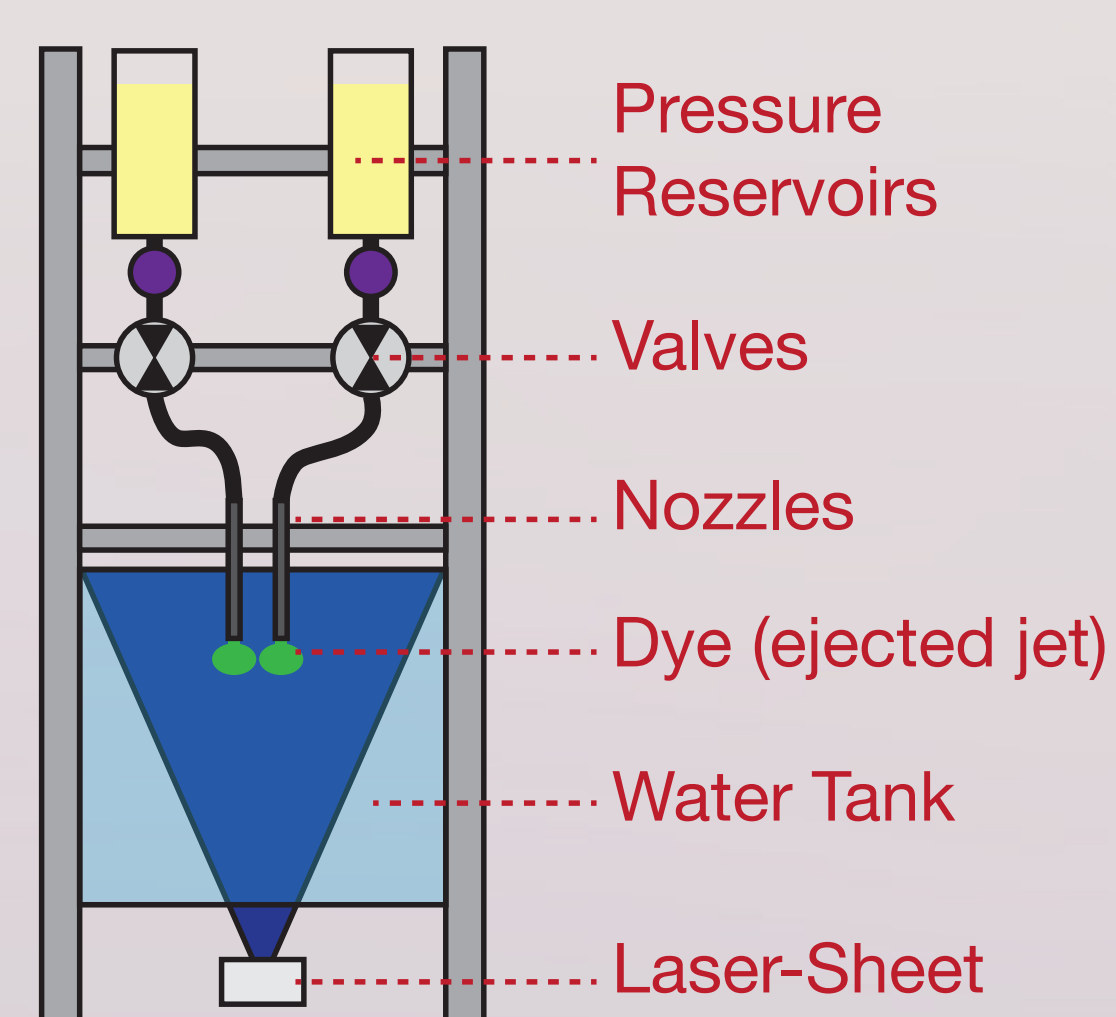
$$T = A_n(\rho u_j^2 + p_n) \approx 2\rho u_{cm} \dot{V}_{cv} + \int_{S_{vb}} p_{vb} \hat{n} \cdot \hat{z} dA$$

Labels in the equation:
 A_n : jet inertia
 ρu_j^2 : overpressure
 $2\rho u_{cm} \dot{V}_{cv}$: vortex ring growth
 $\int_{S_{vb}} p_{vb} \hat{n} \cdot \hat{z} dA$: pressure around vortex ring

Experiment ($Re \approx 350$)

To test the jet interactions, we ejected two jets with variable spacing.

Vortex rings were recorded at high speed using fluorescent dye and a laser.

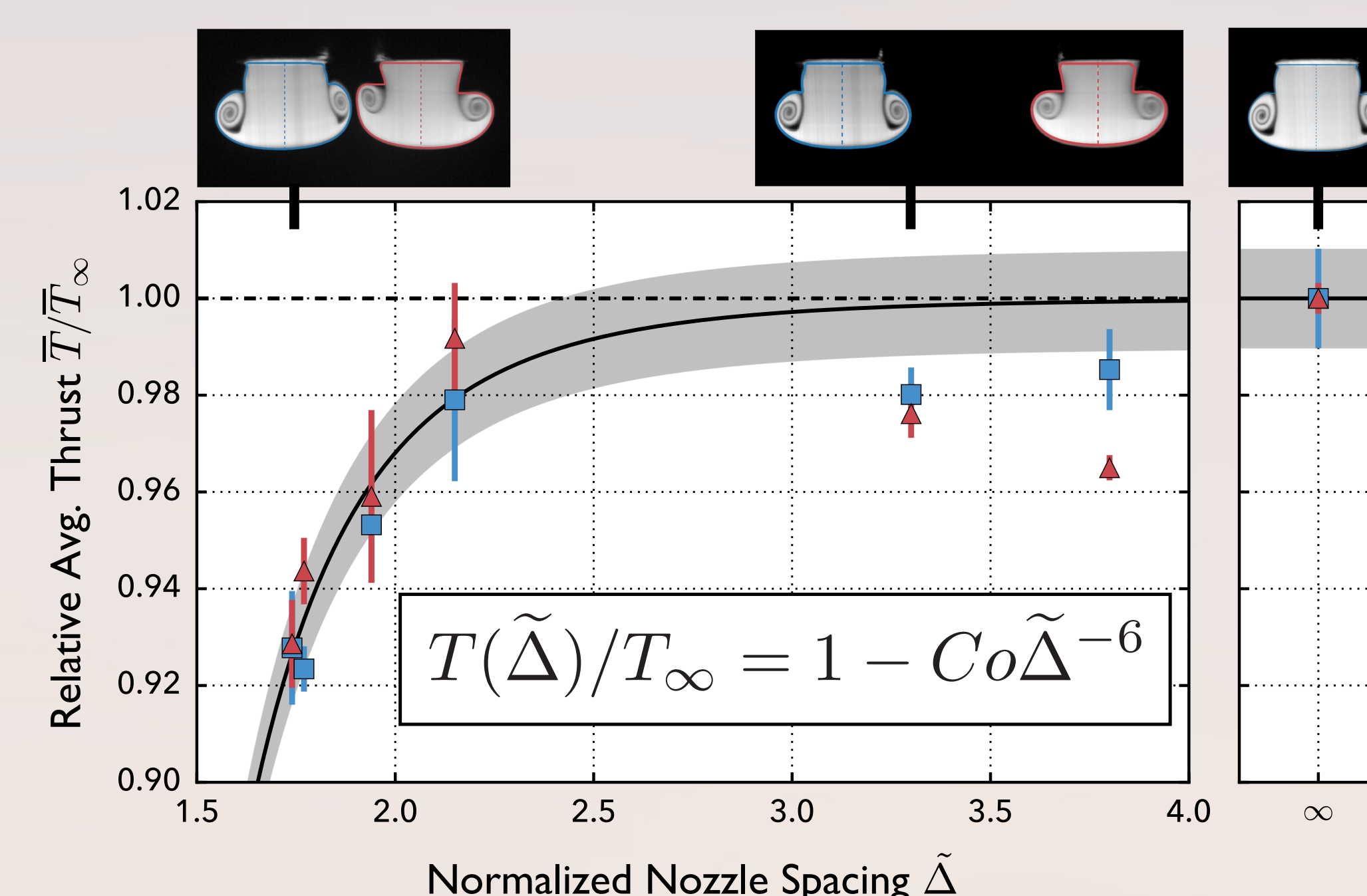


By measuring the **shape**, **size**, and **motion** of the wake, we can estimate **thrust** from the videos.²

Results

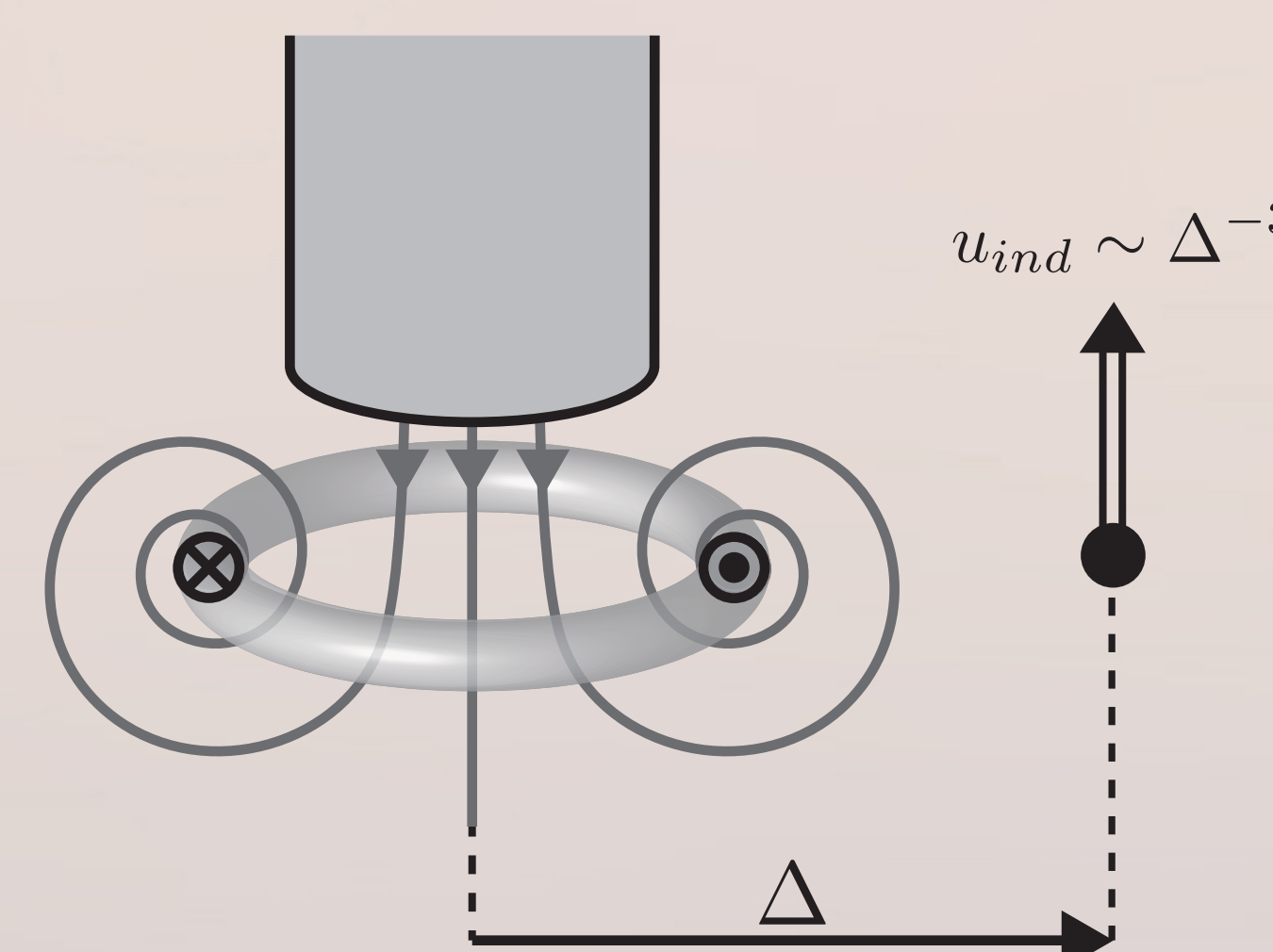
When two jets are pulsed simultaneously, **less thrust** is produced **as the jets get closer**.

The thrust drop depends on nozzle spacing, nozzle diameter, and a dimensionless coupling coefficient, $Co = 2.04$



Our Interaction Model

What's the physics behind the observed behavior?



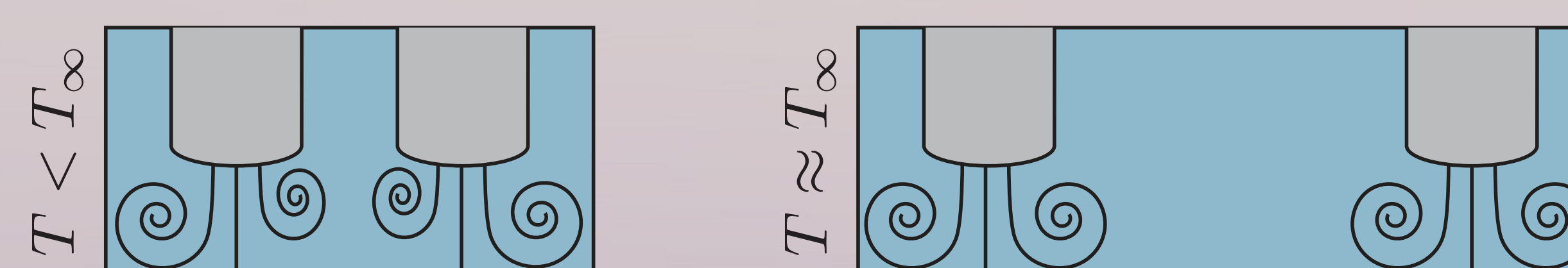
By considering that the jets will interact during formation through **vortex induction**, we predict that the thrust should change according to:

$$T \sim \rho u_{ind}^2 \sim \tilde{\Delta}^{-6}$$

To understand why the thrust drops as the nozzles get closer, consider how the **streamlines** behave.

When the jets are closer, the symmetry requires that the nozzle **streamlines straighten, decreasing the overpressure**.

Since the jet velocity is constant, **less thrust is produced**.



Conclusions

- ① For nearby pulsed jets, **vortex interactions** between the jets force the streamlines to straighten, and thus **generate less thrust**.
- ② This **effect is highly localized**, scaling as $\tilde{\Delta}^{-6}$.
- ③ Our model suggests that careful **control of jet timing** could **enhance thrust production**, similar to how jellyfish exploit stopping vortices for efficient propulsion.
- ④ These results can be generalized to more nozzles for first order performance estimates.

More details can be found in our paper:

Effects of multijet coupling on propulsive performance in underwater pulsed jets. Phys. Rev. Fluids, 1, 034501. (2016)



For a different view of this project, check out my **YouTube** video with Nicole from **FYFD**!



References

- (1) Mohseni, K. Pulsatile vortex generators for low-speed maneuvering of small underwater vehicles. *Ocean Engineering*, **33**, 2209 (2006).
- (2) Ruiz, L. A., Whittlesey, R. W. & Dabiri, J. O. Vortex-enhanced propulsion. *Journal of Fluid Mechanics* **668**, 5-32 (2010).
- (3) Krueger, P. S. & Gharib, M. The significance of vortex ring formation to the impulse and thrust of a starting jet. *Physics of Fluids* **15**, 1271 (2003).

